

Star Origami

The Starrygami™ Galaxy of Modular
Origami Stars, Rings and Wreaths

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Boca Raton and London

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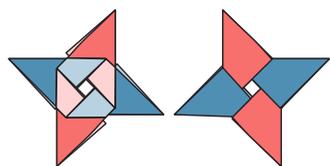
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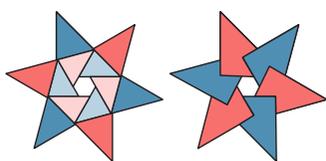
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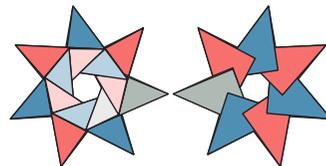
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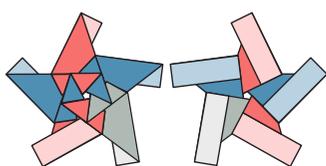
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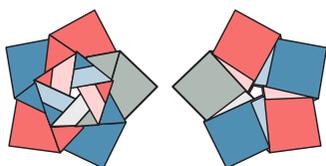
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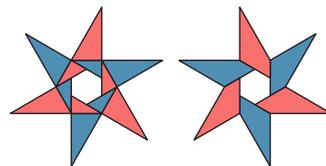
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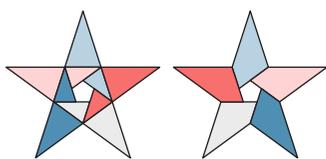
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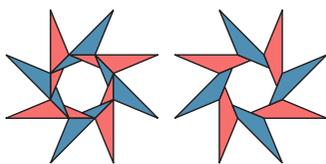
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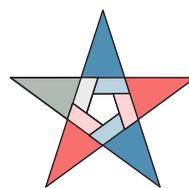
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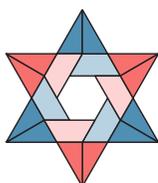
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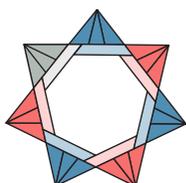
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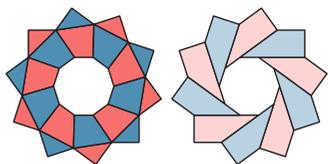


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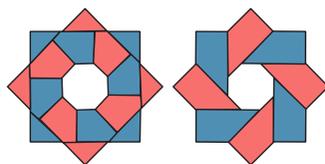
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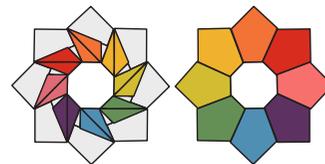
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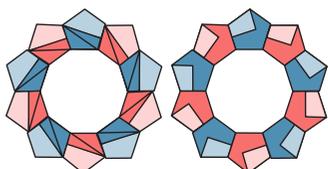
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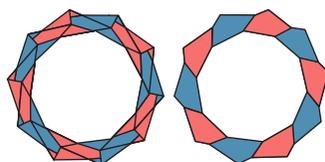
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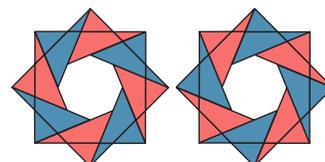
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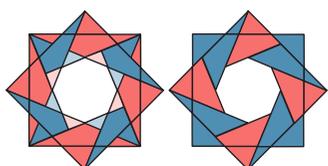
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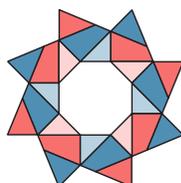
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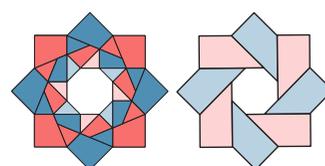
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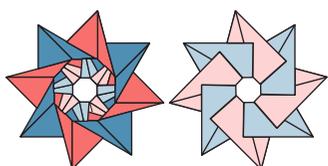
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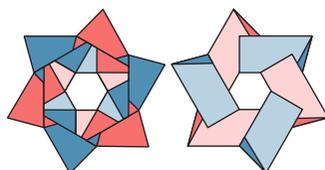
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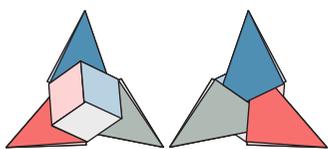
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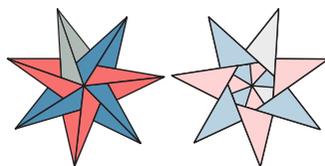
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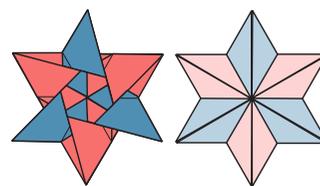
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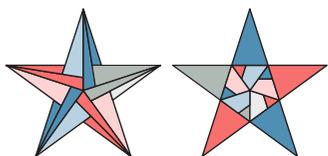
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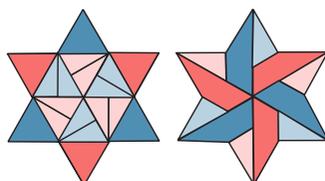
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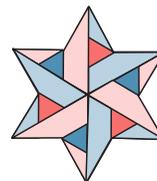
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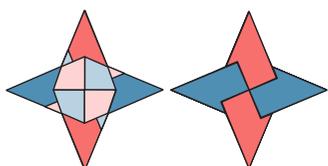
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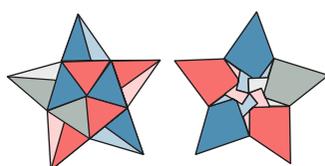
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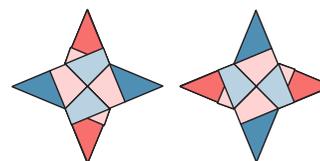
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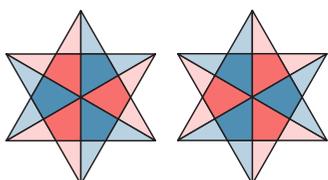
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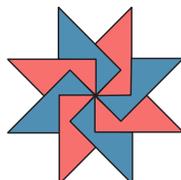
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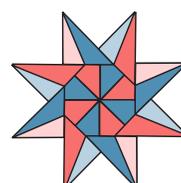
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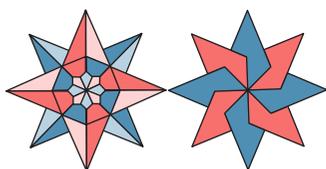
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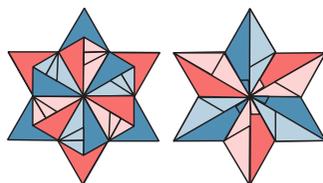
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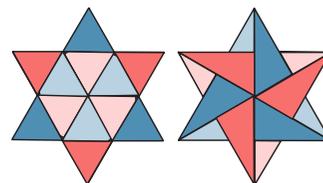
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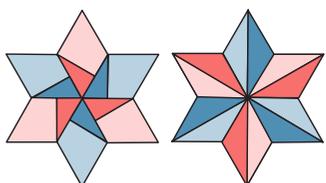
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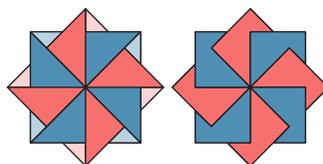
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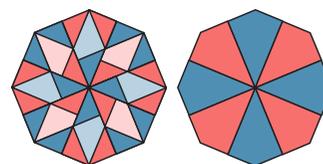
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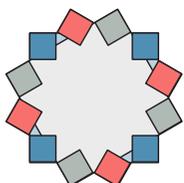
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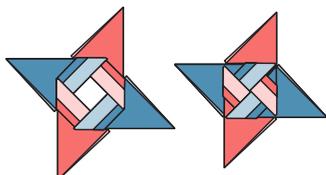


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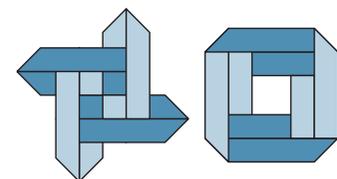


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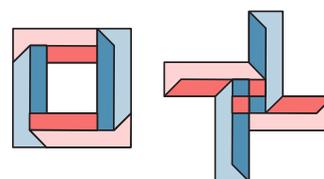
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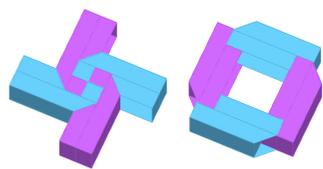
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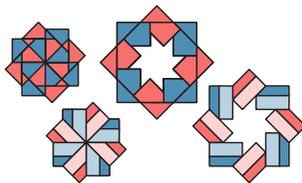
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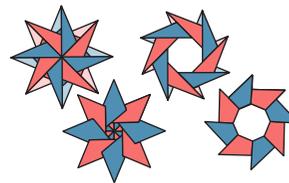
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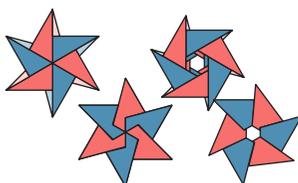
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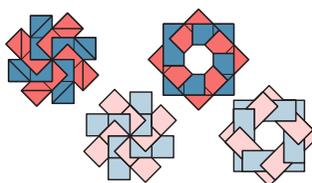
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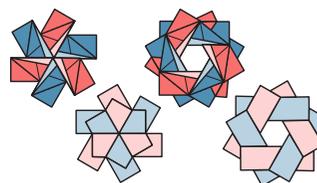
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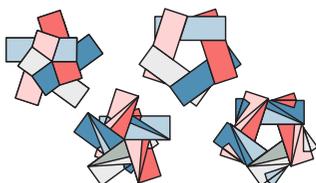
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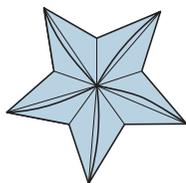


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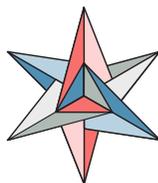


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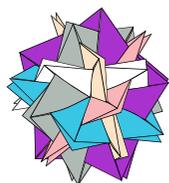
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About the Author

Tung Ken Lam is an origami creator, author and qualified mathematics teacher. His best-known works are *WXYZ* (p. 110) and *Jitterbug*.

He is the author of *Action Modular Origami to Intrigue and Delight* (Tarquin, 2018), and coauthor of *Learning Mathematics with Origami* (Association of Teachers of Mathematics, 2016).

His modular creations are fine examples of original and economical folding.

–David Petty, author of *Origami 1-2-3* and *Origami A-B-C*

It has been a long time since I have enjoyed folding so many projects from just one book. The diagrams are among the best I have seen for geometric origami, and the collection of projects is a satisfying variety. Highly recommended! Five out of five stars.

–Michael LaFosse, cofounder of Origamido® Studio and author of over 50 origami books, on *Action Modular Origami to Intrigue and Delight*

He has taught and presented his origami work in France, Italy, Sweden, Japan and USA. He has run many events for teachers, learners and the general public. He accepts commissions for origami projects and creating bespoke origami to order. Clients have included Bletchley Park Trust, The Bodleian Library, University of Oxford, EuroStemCell (formerly the Scottish Centre for Regenerative Medicine) and Honda UK.



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